



*Math in Focus: Singapore Math* National Institute  
July 16-17 2013 | Philadelphia PA

# ADVANCED BAR MODELING



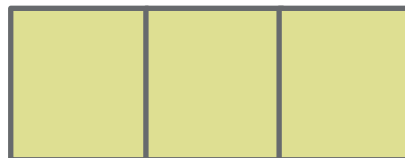
Hoover Herrera, Math In Focus National Specialist

# Advanced Bar Models

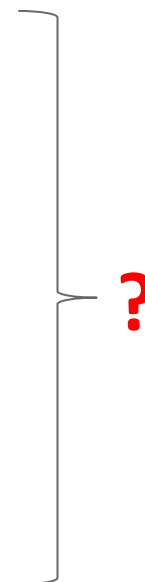
Oranges



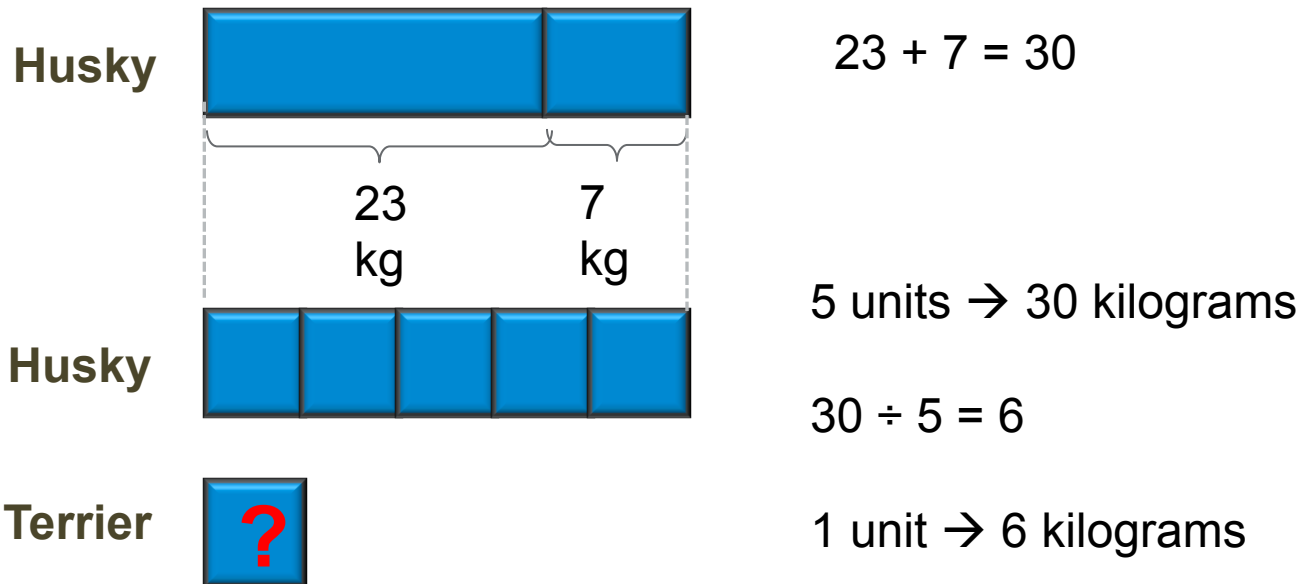
Apples



Peaches

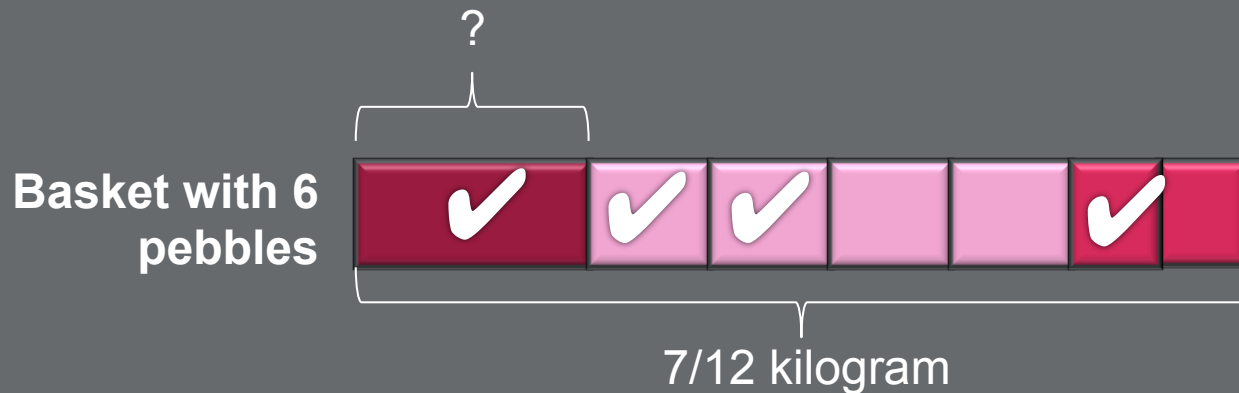


A family has two dogs, a husky and a terrier. The husky's mass is 23 kilograms. If he gains 7 kilograms, his mass will be five times that of the terrier. What is the mass of the terrier?



**The mass of the terrier is 6 kilograms**

The total mass of a basket, 4 large pebbles, and 2 small pebbles is  $\frac{7}{12}$  kilogram. The total mass of the basket, 2 large pebbles and 1 small pebble is  $\frac{5}{12}$  kilogram. Find the mass of the empty basket.



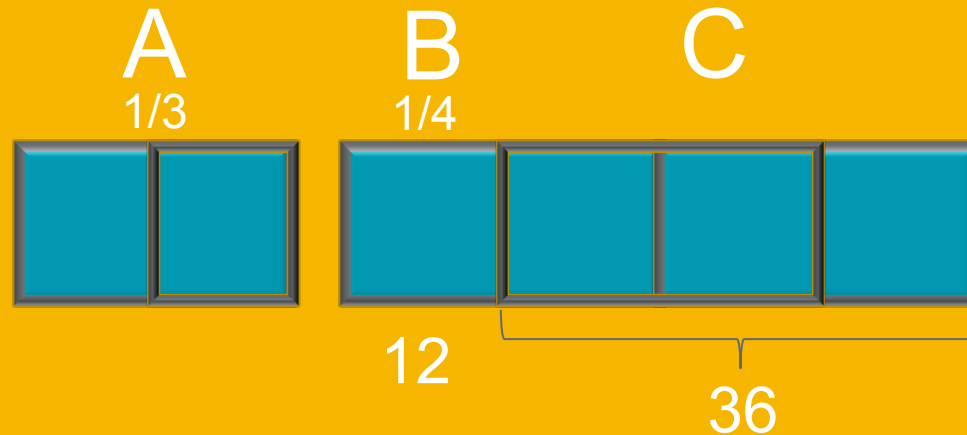
$$\frac{7}{12} - \frac{5}{12} = \frac{2}{12}$$

$$\frac{5}{12} - \frac{2}{12} = \frac{3}{12}$$

$$\frac{2}{12} = \begin{array}{|c|c|c|} \hline \text{light pink} & \text{light pink} & \text{dark red} \\ \hline \end{array} \quad \& \quad \frac{3}{12} \text{ or } \frac{1}{4} = \begin{array}{|c|} \hline \text{dark red} \\ \hline \end{array}$$

The mass of the empty basket is  $\frac{1}{4}$  kilograms.

Roy took a test with 3 sections A, B, and C. Roy spent  $\frac{1}{3}$  of his time on Section A and  $\frac{1}{4}$  of the remaining time on Section B. He spent 36 minutes on section C. How much time did Roy take to complete the whole test?



$$36 = \frac{3}{4}, \text{ so } 36 \div 3 = 12$$

$$\frac{1}{3} = \frac{2}{6} = 24, \quad \frac{6}{6} = 72$$

**He spent 72 minutes on the test.**

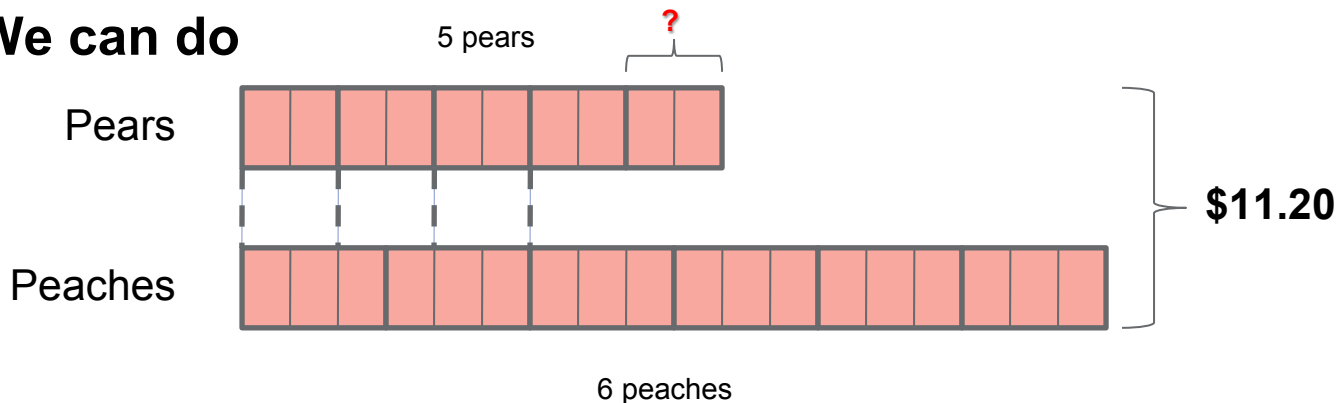
Jordan paid \$11.20 for 5 pears and 6 peaches.  
 The cost of 3 pears is as much as 2 peaches.  
 Find the cost of a pear.

**Solution:** What do we know? What can we do?

**We know that**



**We can do**



$$28 \text{ units} = 11.20$$

$$11.20 \div 28 = 0.40$$

$$1 \text{ unit} = 0.40$$

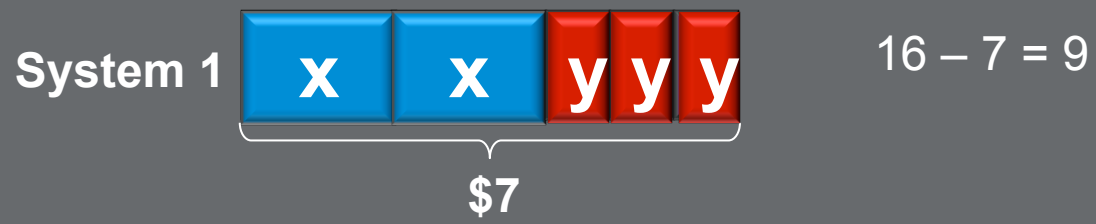
$$2 \text{ units} = \$0.80$$

(a pear)

**The cost of a pear is \$0.80.**



Two notepads and three pens cost \$7. One notepad and 6 pens cost \$8. What is the cost of one notepad and one pen?

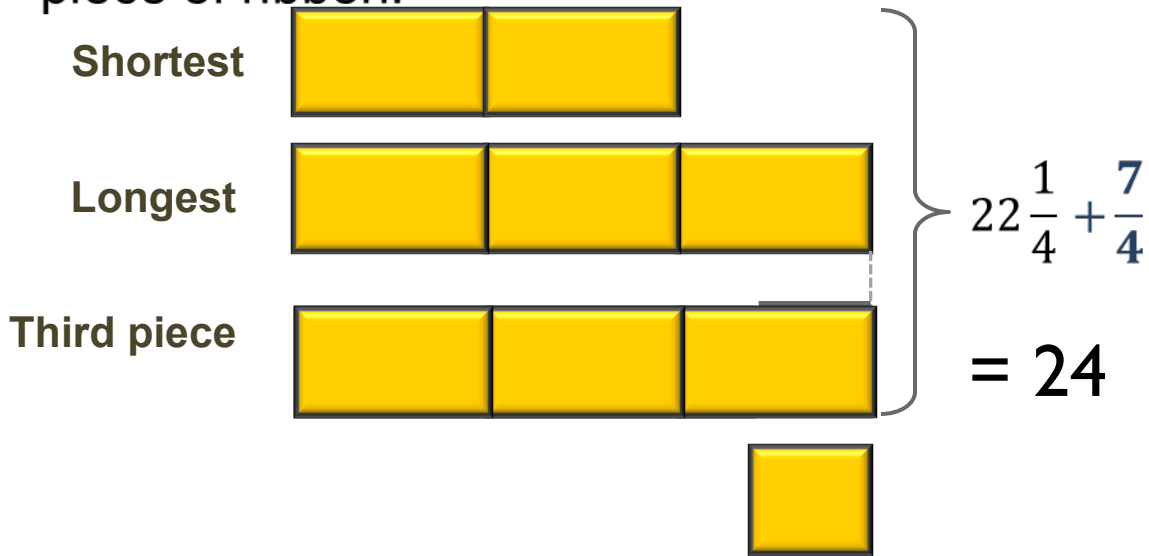


9 units = 9  
1 unit = 1

y = pen = \$1  
x = notebook = \$2

One notebook is \$2 and the cost of one pen is \$1.

Margaret buys a roll of ribbon from a shop. She cuts the ribbon into three pieces. The ratio of the length of the shortest piece to the length of the longest is 2 : 3. The third piece is  $1\frac{3}{4}$  feet shorter than the longest piece. If the total length of the ribbon is  $22\frac{1}{4}$  feet long, then find the length of each piece of ribbon.



8 units = 24 feet  
 1 unit = 3 feet

**Shortest** 2 units  $\times$  3 feet = **6 feet**  
**Longest** 3 units  $\times$  3 feet = **9 feet**  
**Third piece** 9 feet -  $\frac{7}{4}$  =  **$7\frac{1}{4}$  feet**

$$2x + 3x + (3x - 1\frac{3}{4}) = 22\frac{1}{4}$$

$$8x - 1\frac{3}{4} = 22\frac{1}{4}$$

$$8x - 1\frac{3}{4} + 1\frac{3}{4} = 22\frac{1}{4} + 1\frac{3}{4}$$

$$8x = 24$$

$$\frac{8x}{8} = \frac{24}{8}$$

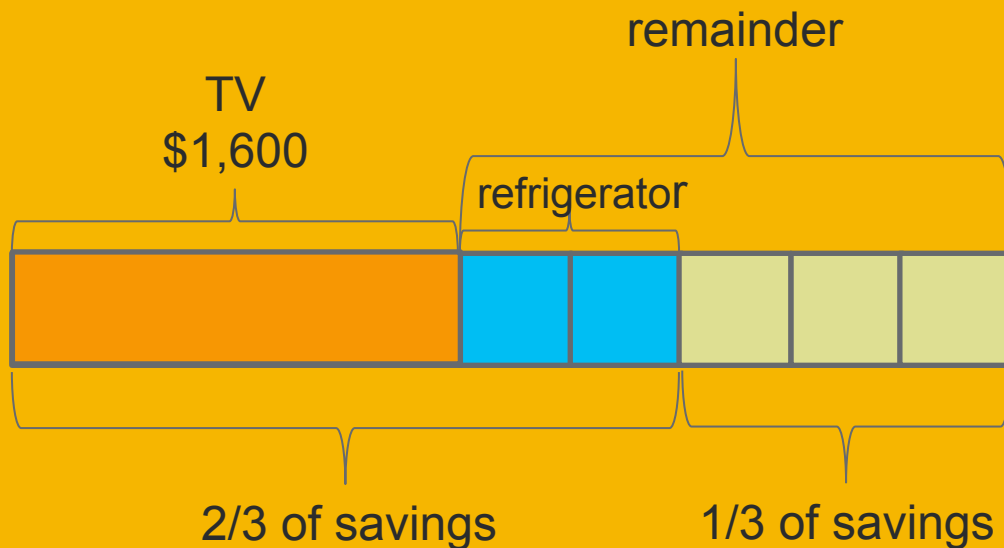
$$x = 3$$



Mr. Thomas spent \$1,600 of his savings on a television set and  $\frac{2}{5}$  of the remainder on a refrigerator. He had  $\frac{1}{3}$  of his original amount of savings left.

A) What was Mr. Thomas's original savings?

B) What was the cost of the refrigerator?



$$4 \text{ units} \rightarrow \$1,600$$

$$1 \text{ unit} \rightarrow = \$400$$

$$9 \times \$400 = \$3,600$$

$$2 \times \$400 = \$800$$

**The original savings were \$3,600 and the refrigerator cost \$800.**



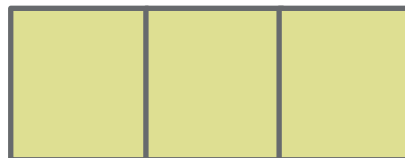
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